

Spring 2014/2015

Math 1300–Precalculus Final Exam

Your Name: _____

Instructions: Please justify all your answers. No partial credit will be awarded for answers without calculations or explanations. You may **Not** use any electronic technology. Please sign your name below signifying that you have read, understood and will abide by these directions and will not cheat.

Your Signature: _____

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | Total |
|-----------------|---|---|----|----|---|----|----|----|----|----|----|----|-------|
| Possible Points | 6 | 6 | 10 | 15 | 6 | 10 | 10 | 10 | 12 | 15 | 20 | 10 | 130 |
| Your Scores | | | | | | | | | | | | | |

Problem 1: (6 points) Given that $\tan(\theta) = 4$ and $\sec(\theta) < 0$, find the exact values of the six circular functions evaluated at θ .

$$\sin(\theta) = \underline{\hspace{2cm}} \quad \sec(\theta) = \underline{\hspace{2cm}}$$

$$\cos(\theta) = \underline{\hspace{2cm}} \quad \csc(\theta) = \underline{\hspace{2cm}}$$

$$\tan(\theta) = 4 \quad \cot(\theta) = \underline{\hspace{2cm}}$$

Problem 2: (6 points) Find the quotient and remainder when the polynomial $7x^4 - 5x^3 + 3x - 1$ is divided by $x - 2$.

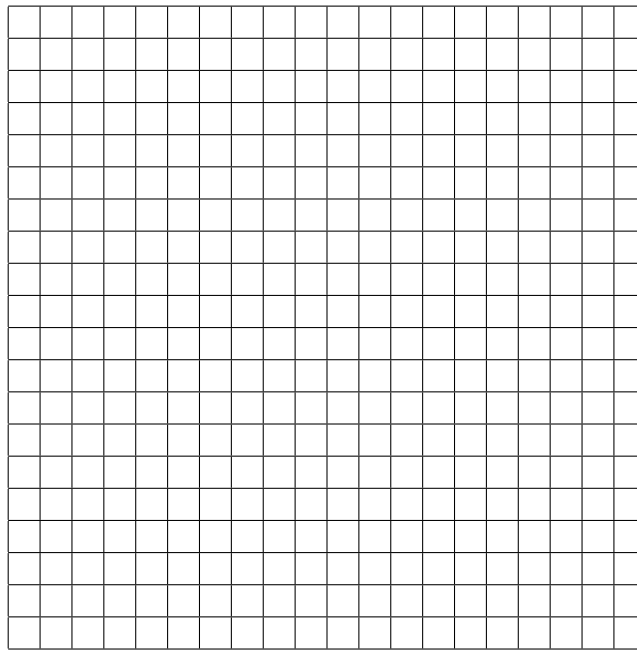
Problem 3: (10 points) Solve

$$2 \sin^2(x) = \sin(x) \quad \text{on} \quad [0, 2\pi]$$

Problem 4: (15 points) Consider the equation

$$9x^2 - 4y^2 - 36x - 24y - 36 = 0$$

- (1) Put the equation in standard form and identify as a type of conic section.
- (2) Graph the equation, label the foci, vertices and center.



Problem 5: (6 points) Find the exact values of

(1) $\arccos\left(-\frac{\sqrt{3}}{2}\right)$

(2) $\arcsin\left(-\frac{1}{2}\right)$

Problem 6: (10 points)

- (1) Use the properties of logarithms to re-write the expression

$$\log_2(x^3 - 4) + 2\log_2(x + 2) - 4\log_2(3x + 2)$$

as a single logarithm.

- (2) Use the properties of logarithms to re-write the expression

$$\log_3 \left(\frac{xy}{z^2 \sqrt[3]{w}} \right)$$

so that the result does not contain any powers, products or quotients.

Problem 7: (10 points) Solve the inequality and express your answer in interval notation.

$$x + |2x - 3| < 2$$

Problem 8: (10 points) Use angle sum, angle difference or half angle identities to find the exact values of

(1) $\cos\left(\frac{\pi}{12}\right)$

(2) $\sin\left(\frac{5\pi}{12}\right)$

Problem 9: (12 points) Consider the function

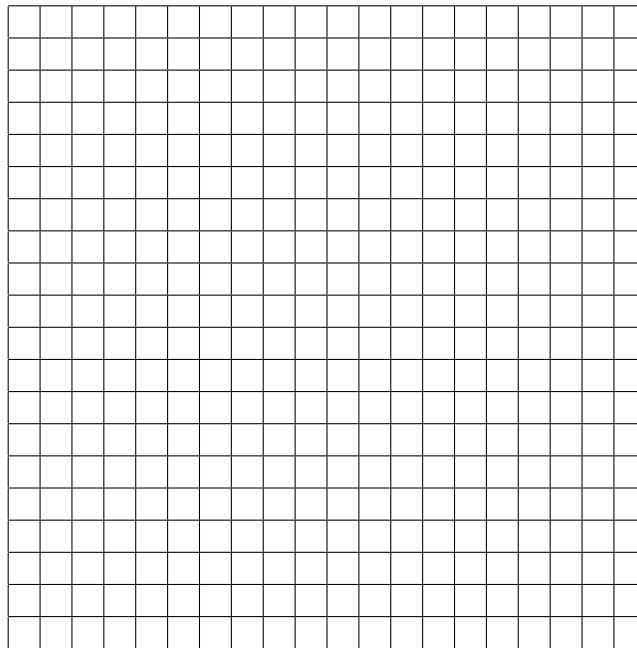
$$f(x) = \frac{3x - 7}{x - 1}$$

- (1) Find the domain of $f(x)$, write your answer in interval notation.
- (2) Show that $f(x)$ is one to one on its domain.
- (3) Find an explicit formula for the inverse function $f^{-1}(x)$.
- (4) Verify your formula is correct by computing and simplifying $f \circ f^{-1}(x)$.

Problem 10: (15 points) Determine the values of c for which the function

$$f(x) = x^2 - 2x + c$$

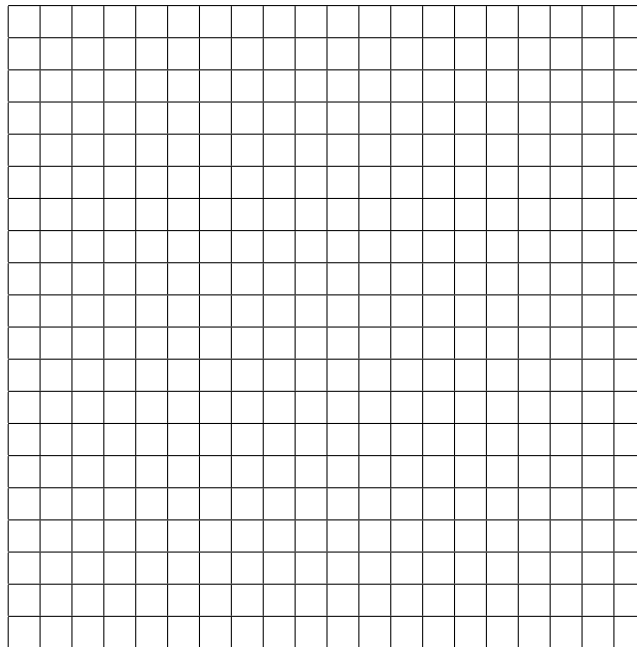
- (1) Has a unique real root. Express your answer in set notation and graph this case below.
- (2) Has exactly two distinct real roots. Express your answer in interval notation.
- (3) Has no real roots. Express your answer in interval notation.



Problem 11: (20 points) Consider the rational function

$$f(x) = \frac{x^2 + 4x + 3}{x^2 - 1}$$

- (1) Express the domain of f in interval notation.
- (2) Find the x and y intercepts of f .
- (3) Find all vertical and horizontal asymptotes.
- (4) Identify any holes.
- (5) Sketch a detailed graph of f .



Problem 12: (10 points) Use the method of transformations to sketch a detailed graph of

$$g(x) = 3 - 2f(x - 1)$$

where the graph of

$$f(x) = (x - 1)^2(x + 3)^2$$

is shown below. Track the four points indicated on the graph of $f(x)$ through the transformation.

