Recall the definition of the derivative:\[ f'(x) = \lim_{h \to 0} \frac{f(x+h)-f(x)}{h} \]

Let \[ f(x) = \frac{3x+5}{x+7} \]

Find \( f'(x) \) using the definition of the derivative. Show all details clearly and explain key steps.