A right circular cylinder is inscribed in a cone with base radius $r$ and height $h$. The cylinder has base radius $a$ and height $b$.

(a) What are the dimensions $a, b$ of the cylinder with the largest possible volume?
(b) What is the largest possible volume of the cylinder?

(Show all details of the calculation clearly & use correct notation.)